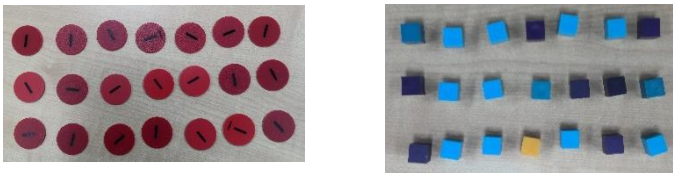
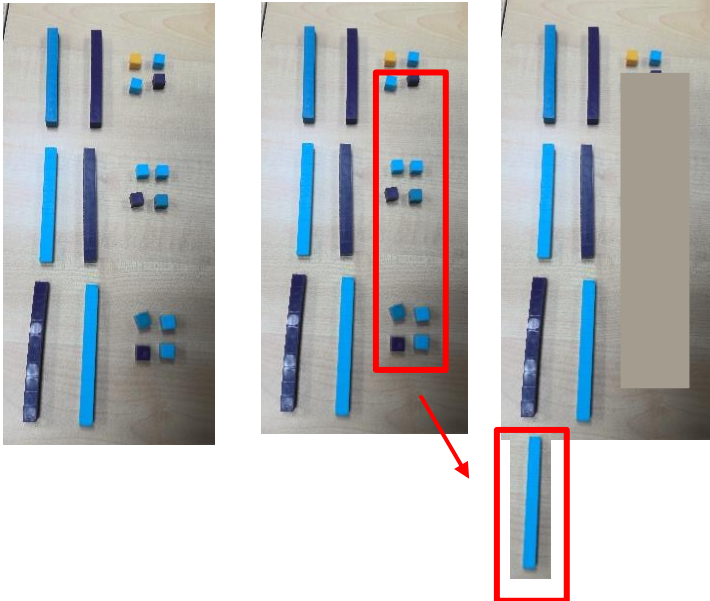


Fair Oak Junior School Calculation Policy (multiplication and division)

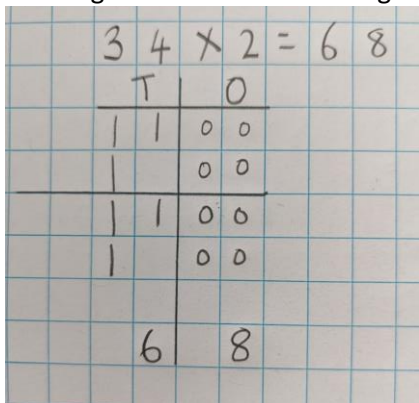
Progression with formal methods for multiplication and division

Multiplication

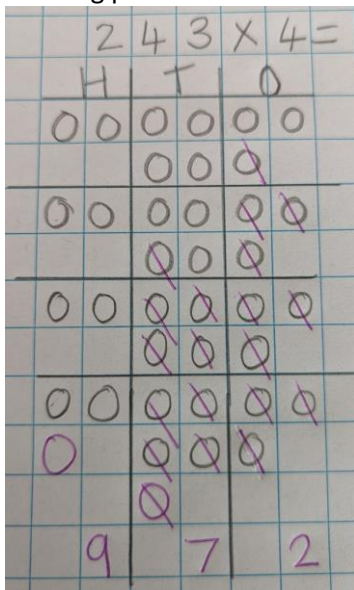
What the method looks like	Language used to teach it
<p><u>Arrays (1-digit)</u></p> <p>$3 \times 7 = 21$</p> 	<ul style="list-style-type: none"> • 3 and 7 are our factors. When we multiply our factors we get a product. • Multiplication is commutative so we can swap our factors round and we would get the same answer • $3 \times 7 = 21$ • $7 \times 3 = 21$ • To make an array we are making 7 groups of 3 or 3 groups of 7
<p><u>Partition and multiply with dienes/ place value counters (2-digit)</u></p> <p>$24 \times 3 =$</p> 	<ul style="list-style-type: none"> • 24 is the first factor and because it is the greatest number we are going to make 3 groups. • We make the factor (24) 3 times (you can use a tens and ones column to support if it helps children partition accurately) • We add the ones to get 12 ones. • We exchange ten ones for one ten • We add our tens to get 70 so our product is 72

Partition and multiply by drawing

Drawing dienes with no exchange

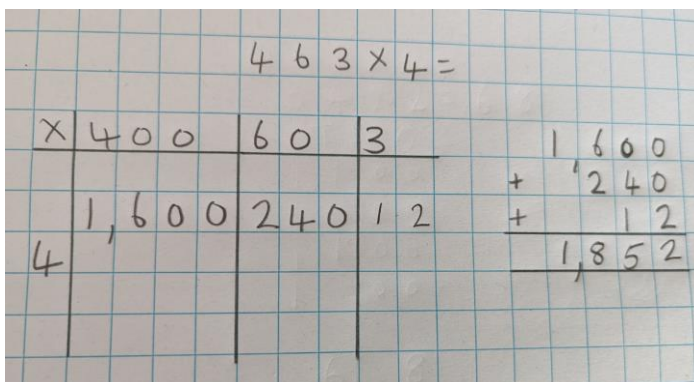


Drawing place value counters with exchange



Grid method

Before children can do this method, they need to be able to scale number facts by 10, 100, 1000 etc. e.g. $3 \times 5 = 15$ so $3 \times 50 = 150$



- Make the greatest factor by the other factor (number of groups)
- For 34×2 we add the ones then tens
- For 243×4 we add the ones to get 12 ones.
- We exchange ten ones for one ten
- We add the tens to get 17 tens
- We exchange ten tens for one hundred
- We add the hundreds to get 9 hundreds
- We have a product of 972

- Our calculation is 463×4
- We draw a grid to be able to partition our number
- We write out the partitioned number
- We multiply the hundreds by the other factor (4)
- We can do this by scaling number facts. I know 4×4 is 16 so if one of my factors is multiplied by 100, I multiply the product by 100 to get 1,600
- I multiply my tens by 4 and my ones by 4
- I add these up in column method

Expanded formal method

$$\begin{array}{r} 3,724 \times 3 = \\ \text{Th H T O} \\ 3,724 \\ \times \quad 3 \\ \hline 12 \quad (3 \times 4) \\ 60 \quad (3 \times 20) \\ 2,100 \quad (3 \times 700) \\ 9,000 \quad (3 \times 3,000) \\ \hline 11,172 \\ \times \end{array}$$

- This method is similar to the grid method in the way the number is partitioned but the way it is written means it is ready for column addition
- We write out the brackets of the partitioned calculations
- We multiply our ones, tens, hundreds then add these up in column method
- We get a product of 11,172

Compact formal method

$$\begin{array}{r} 3724 \times 3 = \\ 3724 \\ \times \quad 3 \\ \hline 11172 \\ \times \end{array}$$

- We write out our calculation
- We multiply out ones. 3×4 is 12 so we exchange ten ones for one ten and write this in the tens column underneath the line.
- We multiply our tens to get 6 tens and add on the exchanged ten and cross this out to get 7 tens
- We multiply the hundreds and thousands, exchanging as we go
- We get a product of 11,172

Grid method with 2-digit numbers (from year 5)

- This is the same as the grid method with 1-digit numbers apart from we have two rows as we are multiplying by a two-digit number. We partition both factors and multiply the parts together in the grid
- We then add these up in formal column method for addition

$$562 \times 23 =$$

x	500	60	2
20	10,000	1,200	40
31,500	1,800	6	

	10,000
+	1,500
+	1,200
+	180
+	40
+	6
	12,926

Expanded formal method with 2-digit numbers (from year 5)

$$562 \times 23 =$$

	562
x	23
	6 (3 x 2)
	180 (3 x 60)
	1,500 (3 x 500)
	40 (20 x 2)
	1,200 (20 x 60)
	10,000 (20 x 500)
	12,926

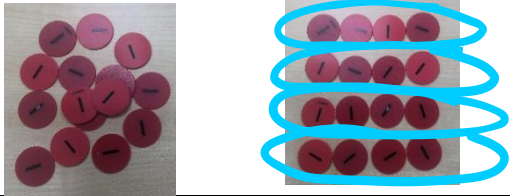
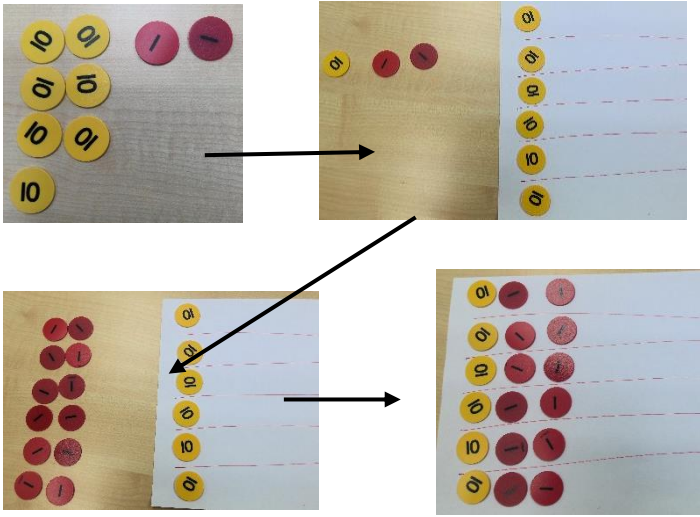
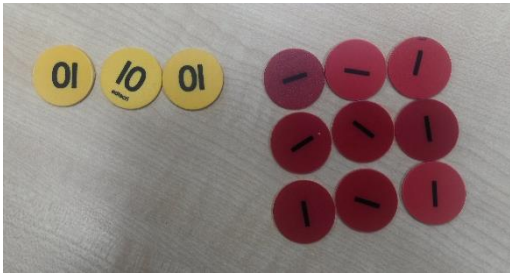
- The same partitioned calculations as above, but written in a formal way so the numbers can be added up with column method.
- We write the calculations in brackets on the right
- If children do not write out the calculations, they often don't line the numbers up correctly.

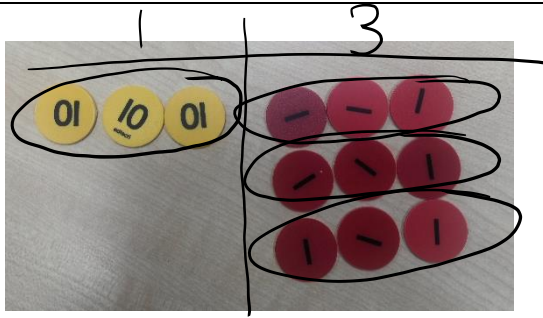
Compact formal method with 2-digit numbers (from year 5)

$$\begin{array}{r} 562 \times 23 = \\ \underline{ \times 23} \\ 1686 \\ + \times 20 \\ \hline 12806 \end{array}$$

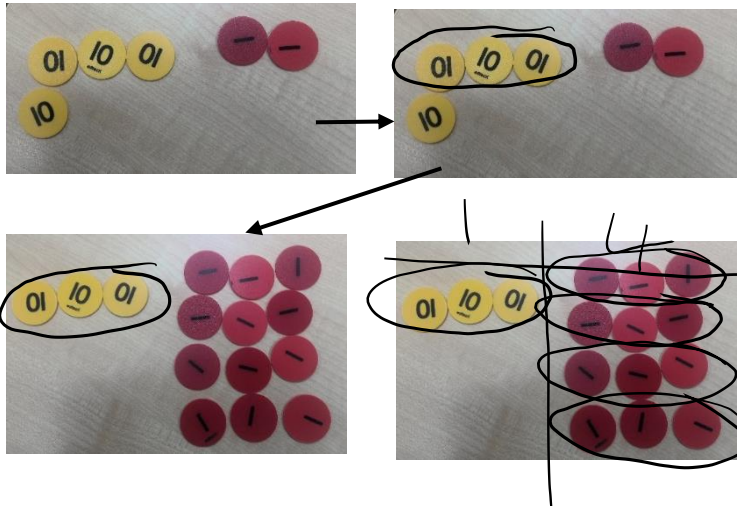
- We write out our calculation of 562×23
- We multiply our 3 by 2 to get 6.
- We multiply 3 by 6 tens to get 18 tens.
- We exchange ten tens for one hundred and write this on the line underneath and write the 8 tens in the tens column
- We multiply 3 by 5 hundreds to get 15 hundreds and add on the extra hundred underneath and cross this out.
- We exchange ten hundreds for one thousand and write this on the line underneath
- We have no thousands to multiply so we move onto the second digit in the factor we are multiplying by
- We multiply 2 tens by 2 to get 40
- We multiply 2 tens by 6 tens to get 120 or 1,200. We exchange ten hundreds for 1 thousand
- We multiply 2 tens by 5 hundreds to get 10,000 and add on the exchanged thousand to get 11 thousands or 11,000.
- We add both the numbers together using formal column method

Division

What the method looks like	Language used to teach it
<p><u>Grouping arrays (1-digit)</u> $16 \div 4 = 4$</p> 	<ul style="list-style-type: none"> • We make our dividend out of dienes ones/ place value counters or counters/ multilink • We group our dividend by the divisor • 16 into groups of 4 • We get a quotient of 4
<p><u>Sharing dienes/ place value counters</u></p> 	<ul style="list-style-type: none"> • The calculation is $72 \div 6$ • We make the dividend • We share the greatest value counters first (in this case tens) into the divisor • We are left with one ten so we exchange one ten for ten ones • We now have 12 ones • We share the ones into the divisor • Each group has 12 • The quotient is 12
<p><u>Grouping dienes/ place value counters (no exchange)</u></p> 	<ul style="list-style-type: none"> • The calculation is $39 \div 3$ • If it is possible, make the tens and ones out into groups of the divisor • You can do this on a place value grid if that supports children • Group the tens. We have one group of the divisor (3) • Group the ones. • We have three groups of the divisor • The quotient is 13

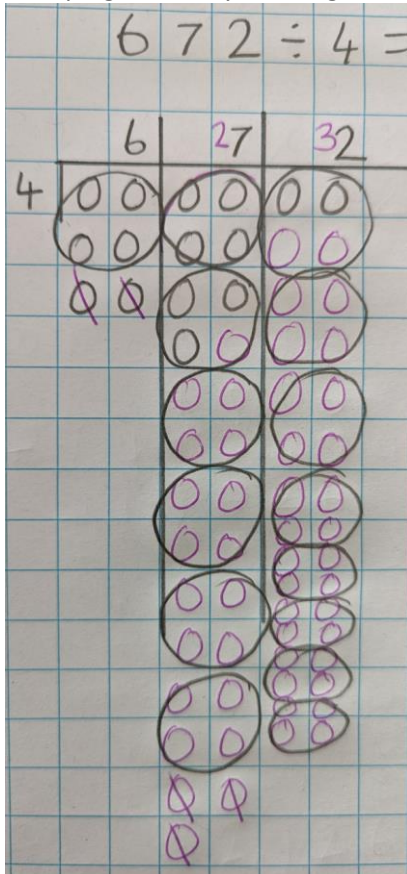


Grouping dienes/ place value counters (with exchange)



- The calculation is $42 \div 3$
- If possible, make the dividend (tens and ones) into groups of the divisor
- Group the tens into groups of the divisor (3)
- We have one ten left so we exchange one ten for ten ones
- We now have 12 ones
- Group the ones
- We have one group of tens and 4 groups of ones
- The quotient is 14

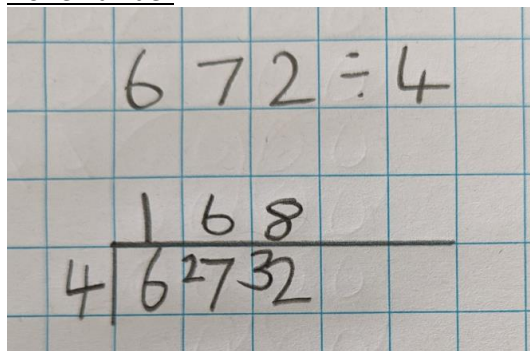
Grouping dienes by drawing



- We draw a place value grid (hundreds, tens and ones) and write our divisor to the left.
- We draw out the hundreds, tens and ones.
- We start with the digit in the highest value column, in this case the hundreds.
- We group the hundreds into groups of the divisor (4)
- There is one group of 4 with 2 hundreds remaining.
- We exchange two hundreds for 20 tens.
- There are 6 groups of 4 tens in 27 tens with 3 remaining
- We exchange 3 tens for 30 ones
- There are 8 groups of 4 ones in 32 ones
- The quotient is 168

Short division (1-digit)

No remainder



- We write the dividend (672) out and draw a division bracket around it
- We write the divisor to the left
- There is one group of 4 hundreds in 6 hundreds with 2 remaining
- We exchange two hundreds for 20 tens
- There are 6 groups of 4 tens in 27 tens
- There are 3 tens remaining which we exchange for 30 ones
- There are 8 groups of 4 ones in 32 ones
- The quotient is 168

Remainder as an integer (whole number)

$$\begin{array}{r} 674 \div 4 \\ 168 \text{ r } 2 \\ \hline 4 \overline{) 674} \end{array}$$

- We write out the dividend (674) and draw a division bracket around it
- We write the divisor to the left
- There is one group of 4 hundreds in 6 hundreds with a remainder of 2 hundreds
- We exchange 2 hundreds for 20 tens
- There are 6 groups of 4 tens in 27 tens with a remainder of 3 tens
- We exchange 3 tens for 30 ones
- There are 8 groups of 4 ones in 34 ones
- The quotient is 168 with a remainder of 2

Remainder as a decimal

$$\begin{array}{r} 674 \div 4 \\ 168.5 \\ \hline 4 \overline{) 674.0} \end{array}$$

- We write out the dividend (674) and draw a division bracket around it
- We write the divisor (4) to the left
- There is one group of 4 hundreds in 6 hundreds with a remainder of 2 hundreds
- We exchange 2 hundreds for 20 tens
- There are 6 groups of 4 tens in 27 tens with a remainder of 3 tens
- We exchange 3 tens for 30 ones
- There are 8 groups of 4 ones in 34 ones with a remainder of 2
- We add a decimal point and a 0 for the tenths column
- We exchange 2 ones for 20 tenths
- There are 5 groups of 4 tenths in 20 tenths
- The quotient is 168.5

Long division (2-digit number – from Year 6)

$19642 \div 23 =$	
00854	$20 + 3 = 23$
23	$40 + 6 = 46$
-184	$60 + 9 = 69$
0124	$80 + 12 = 92$
-115	$100 + 15 = 115$
0092	$120 + 18 = 138$
-92	$140 + 21 = 171$
0	$160 + 24 = 184$
	$180 + 27 = 207$

- We have 19,642 divided by 23
- We write out the 23 times tables
- We can write out the 20 times tables, 3 times tables and add these together
- We write out the dividend 19,642 and draw a division bracket around this
- We write the divisor (23) next to this
- We work out how many groups of 23 in one ten thousand which is 0
- We work out how many groups of 23 in 19 thousands which is 0
- We work out how many groups of 23 in 196 hundreds which is 8
- We subtract 184 (which is 8 groups of 23) from 196 leaving us with a remainder of 12 and put 8 in the hundreds column above the division bracket
- We bring down the 4 next to the 12 remainder
- There are 5 groups of 23 in 124 tens
- We subtract 115 from 124 to give us a remainder of 9 and put 5 in the tens column
- We bring down the 2 next to the 9
- There are 4 groups of 23 in 92
- We put a 4 in the ones column above the division bracket
- We have a quotient of 854